YEAR 9 - REASONING WITH ALGEBRA

@whisto maths

Straight Line Graphs

What do I need to be able to do?

By the end of this unit you should be able to:

- Compare gradients
- Compare intercepts
- Understand and use y= mx + c
- Find the equation of a line from a graph
- Interpret gradient and intercepts of reallife graphs

Keywords

Gradient: the steepness of a line

Intercept: where two lines cross. The y-intercept: where the line meets the y-axis.

Parallel two lines that never meet with the same gradient.

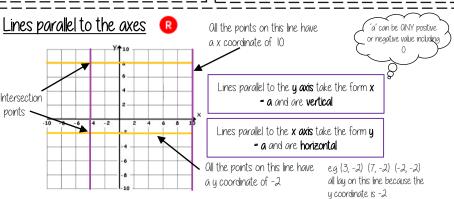
Co-ordinate: a set of values that show an exact position on a graph.

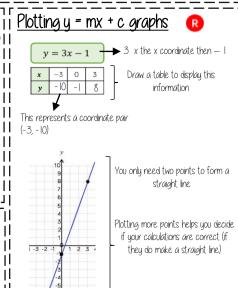
Linear: linear graphs (straight line) — linear common difference by addition/subtraction

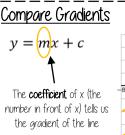
Osymptote: a straight line that a graph will never meet.

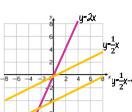
Reciprocal: a pair of numbers that multiply together to give 1.

I I Perpendicular: two lines that meet at a right angle



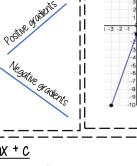




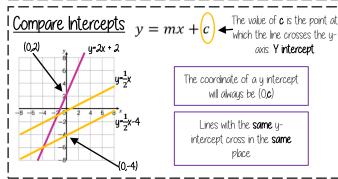


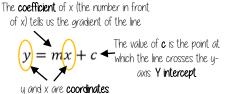
The **areater** the gradient — the steeper the line

> Parallel lines have the same gradient



Remember to join the points to make





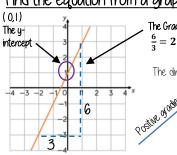
The equation of a line can be rearranged: E.g.: u = c + mx c = y - mxIdentify which coefficient you are identifying or

The u-intercept shows the

minimum charge.

The gradient represents the price per mile

Find the equation from a graph



The Gradient v = 2x + 1

The direction of the line indicates a positive Negative gradients

Real life graphs

y = mx + c

A plumber charges a £25 callout fee, and then £12.50 for every hour. Complete the table of values to show the cost of hiring the plumber.

In real life graphs like this values will always be positive because they

measure distances or objects which cannot be negative

Direct Proportion graphs

To represent direct proportion the graph must start at the origin.

When you have 0 pens this has 0 cost. The gradient shows the A box of pens costs £2.30 Complete the table of values to show the cost of buying boxes of pens. Cost (£) £2.30

YEAR 9 - REASONING WITH ALGEBRA

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Forming and Solving Equations

What do I need to be able to do?

By the end of this unit you should be able to:

- Solve inequalities with negative numbers
- Solve equations with unknowns on both sides |
- Solve inequalities with unknowns on both
- Substitute into formulae and equations
- Rearrange formulae

!!Keuwords

Inequality: an inequality compares who values showing if one is greater than, less than or equal to another

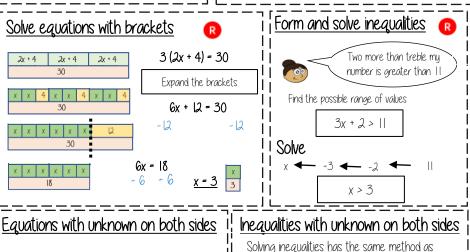
Variable: a quantity that may change within the context of the problem

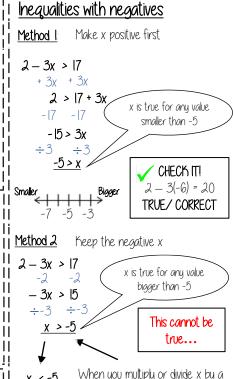
Rearrange: Change the order

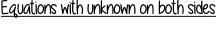
Inverse operation: the operation that reverses the action

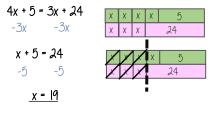
Substitute: replace a variable with a numerical value

Solve: find a numerical value that satisfies an equation









5(x+4)<3(x+2)

5x + 20 < 3x + 6

2x + 20 < 6

Rearrange

5(-8+4)<3(-8+2) 2x < - 14 5(-4)<3(-6) x < -7-20<-18

equations

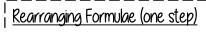
-20 IS smaller than -18

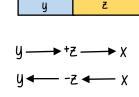
Check it!

Formulae and Equations

Formulae — all expressed in symbols

Equations — include numbers and can be solved |





X = y + Z

Substitute in values

Rearrange to make y the subject. y = x - Z

Using inverse operations or fact families will guide you through rearranging formulae

Rearranging can also be checked by substitution.

Language of rearranging...

Make XXX the subject

Change the subject

Rearranging Formulae (two step) In an equation (find x)

4x - 3 = 9+3 4x = 12

In a formula (make x the subject) xy - s = a

negative you need to reverse the

+ 5 + 5 xu = a + s÷ y ÷ y $X = \underline{a + s}$

The steps are the same for solving and rearranging

Rearranging is often needed when using y = mx + c

e.g. Find the gradient of the line 2y - 4x = 9

Make y the subject first y = 4x + 9Gradient = 4= 2

YEAR 9 - REASONING WITH ALGEBRA

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Testing conjectures

What do I need to be able to do?

By the end of this unit you should be able to:

- Use factors, multiples and primes
- Reason True or False
- Reason Olwaus, sometimes never true
- Show that reasoning
- Make conjectures about number
- Expand binomials
- Make conjectures with algebra
- Explore the 100 arid

Keywords

Multiples: found by multiplying any number by positive integers Factor: integers that multiply together to get another number.

Prime: an integer with only 2 factors.

HCF: highest common factor (biggest factor two or more numbers share)

LCM: lowest common multiple (the first time the times table of two or more numbers match)

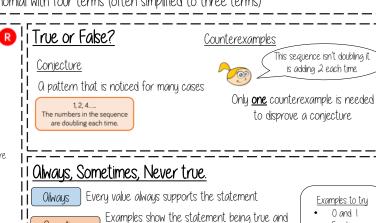
Verify: the process of making sure a solution is correct

Proof: logical mathematical arguments used to show the truth of a statement

Binomial a polynomial with two terms

Quadratic: a polynomial with four terms (often simplified to three terms)

Factors, Multiples and Primes HCF — Highest common factor Multiplication part-whole models HCF of 18 and 30 1, 2, 3, 6, 9, 18 30 30 1, 2, 3, 5, 6, 10, 15, 30 Common factors are factors two or more numbers share LCM - Lowest common multiple LCM of 9 and 12 9, 18, 27, 36, 45, 54 Oll three prime factor trees represent the 12, 24, 36, 48, 60 same decomposition Common multiples are multiples two or more numbers share 📙



counter examples to show when it is false.



No example supports the statement

Examples to try 0 and 1 Fractions Negative numbers

Show that

Numerical verification Show the stages to a solution with numerical values

Olgebraic verification

Show algebraic properties of the solution You may want to use pictorial images to support this

Olgebra tiles

Proof

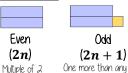
Expandina binomials

 $2(x+2) \equiv 2x+4$

Simple proofs using algebra

Compare the left hand side of an equation with the right hand side — are they the same or different?

Conjectures



Use numerical verification first Use pictorial verification — the representations of numbers of odd and even

Exploring the 100 square

In terms of n' is used to make generalisations about relationships between numbers

11 12 13 14 15 16 17 18 19 30 24 25 27 28 29 22 23 26 32 33 34 35 36 37 38 39 49 50 41 42 43 44 45 46 47 48 54 55 56 57 58 59 64 65 66 67 68 69 70 61 62 63 71 72 73 74 75 76 77 78 79 80 82 83 84 85 86 87 88 89 92 95 96

Positions of numbers in relation to n form expressions. E.g. one space to the right of nn + 1

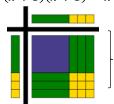
E.g. One row below nn + 10

The size of the grid for

generalisation changes the

relationship statements

$(x+3)(x+3) \equiv x^2 + 6x + 9$



This is a quadratic. It has four terms which simplified to three terms

Olgebra tiles can

expansion

Has two terms

represent a binomial

The order of the binomial has no impact on the outcome eg (x + 3)(3 + x)

Positive values

YEAR 9 - CONSTRUCTING IN 2D/3D

@whisto maths

3D Shapes

What do I need to be able to do?

By the end of this unit you should be able to:

- Name 2D & 3D shapes
- Recognise Prisms

Parallelogram/ Rhombus Base x Perpendicular height

Orea of a trapezium

(a+b)xh..

- Sketch and recognise nets
- Draw plans and elevations
- Find areas of 2D shapes
- Find Surface area for cubes, cuboids, triangular prisms and culinders
- Find the volume of 3D shapes

Keywords

2D: two dimensions to the shape e.g. length and width

3D: three dimensions to the shape e.a. length, width and height

Vertex: a point where two or more line segments meet

Edge a line on the boundary joining two vertex

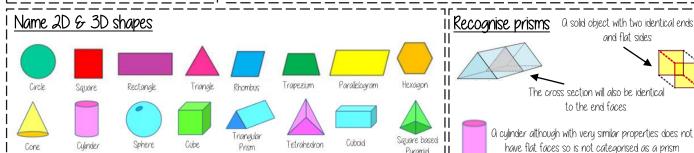
Face: a flat surface on a solid object

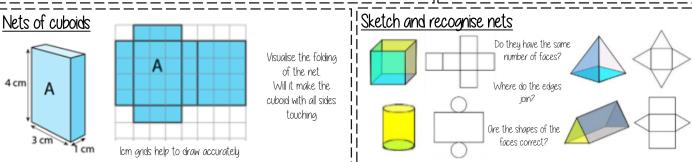
Cross-section: a view inside a solid shape made by cutting through it

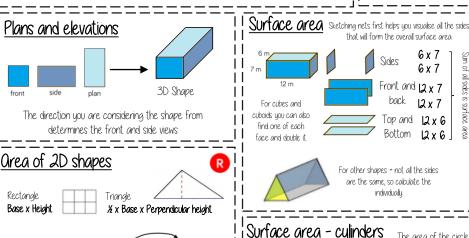
Plan: a drawing of something when drawn from above (sometimes birds eye view)

Perspective: a way to give illustration of a 3D shape when drawn on a flat surface.

Puramid

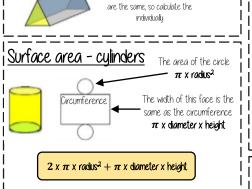


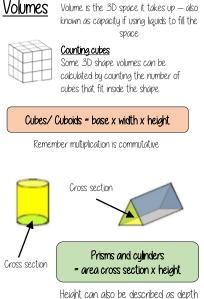




Orea of a circle

 π x radius²





Oreas — square units Oreas and volumes can be Volumes — cube units left in terms of pi π

YEAR 9 - CONSTRUCTING IN 2D/3D.

@whisto maths

Constructions & congruency

What do I need to be able to do?

By the end of this unit you should be able to:

- Draw and measure angles
- Construct scale drawings
- Find locus of distance from points, lines, two
- Construct perpendiculars from points, lines, anales
- Identify congruence
- Identify congruent triangles

Keywords

Protractor: piece of equipment used to measure and draw angles

Locus: set of points with a common property

Eauidistant: the same distance

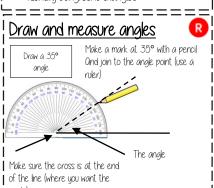
Discorectanale: (a stadium) — a rectangle with semi circles at either end

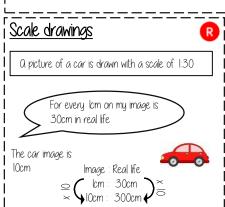
Perpendicular: lines that meet at 90°

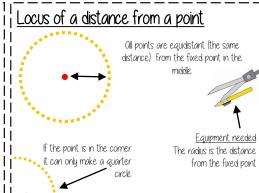
arc: part of a curve

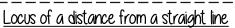
Bisector: a line that divides something into two equal parts

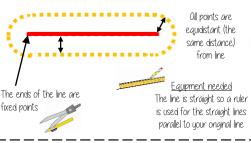
Congruent: the same shape and size











Olso an angle bisector

This cuts the angle in half

From the anale vertex draw two arcs that cut the lines forming the angle

Keep the compass the same size and use

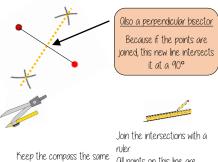
the new arcs as centres to draw

Join the vertex to the intersection

intersecting arcs in the middle

ocus of a distance from two lines

Locus equidistant from two points



Keep the compass the same Oll points on this line are size and draw two arcs from equidistant from both points

Construct a perpendicular from a point

Use a compass and draw an arc that cuts the line. Use the point to place the compass

Keep the compass the same distance and now use uour new points to make new interconnecting arcs

Connectina the arcs makes the bisector

Conaruent fiaures



Congruent figures are identical in size and shape — they can be reflections or rotations of each

Congruent triangles

Side-side-side

Oll three sides on the triangle are the same size

Ongle-side-angle

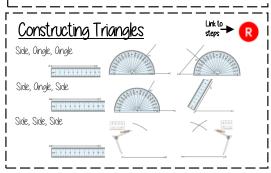
Two angles and the side connecting them are equal in two triangles

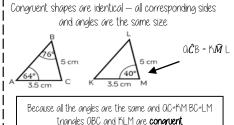
Side-angle-side

Two sides and the angle in-between them are equal in two triangles (it will also mean the third side is the same size on both shapes)

Right angle-hypotenuse-side

II The triangles both have a right angle, the hypotenuse and one side are the same





YEAR 9 - REASONING WITH NUMBER

@whisto maths

Numbers

 \bigcirc = 1

The act of counters

into their

negative is turning

them over

What do I need to be able to do?

By the end of this unit you should be able to:

- Identify integers, real and rational numbers
- Work with directed number
- Solve problems with number
- Find HCF/ LCM
- Odd/ Subtract fractions
- Multiply/ Divide fractions
- Write numbers in standard form

Keywords

Integer: a whole number that is positive or negative

Rational: a number that can be made by dividing two integers

Irrational: a number that cannot be made by dividing two integers

Inverse operation: the operation that reverses the action

Quotient: the result of a division

Product: the result of a multiplication.

Multiples: found by multiplying any number by positive integers

Factor: integers that multiply together to get another number

Integers, real and rational numbers

Rational — root word: ratio

Real numbers: $\frac{2}{3}$ stems from 2:1 ($\frac{2}{3}$ of the whole)

Irrational numbers: $\sqrt{2}$ the solution is a decimal that never ends and does not repeat.

The square root of a negative is not a real number and cannot be found



Common factors are factors two or more numbers share

HCF — Highest common factor

HCF of 18 and 30



LCM — Lowest common multiple

LCM of 9 and 12

9, 18, 27, 36, 45, 54

12, 24, 36, 48, 60

I CM = 36

The first time their multiples match

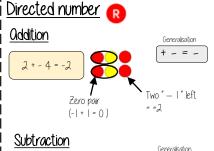
Standard form

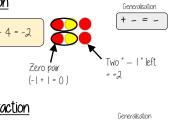
any number A x 10 n between I and less than 10

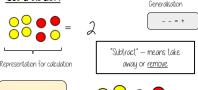
 $(1.5 \times 10^5) \div (0.3 \times 10^3)$ 6 x 105 + 8 x 105

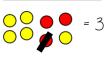
- = 600000 + 800000
- = 1400000
- $15 \div 0.3 \times 10^5 \div 10^3$
- = 1.4 x 10⁵

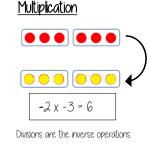
 $=5 \times 10^{2}$

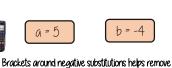








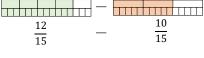


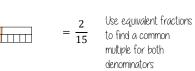


calculation errors $2a - b = 2 \times 5 - (-4) = 10 + 4 = 14$

Addition/Subtraction of fractions 👩

Take away one

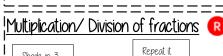


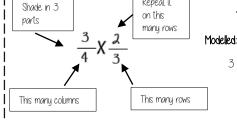


Parts shaded

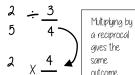
Total number of

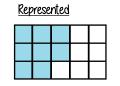
parts in the diagram

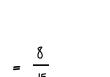




Remember to use reciprocals







YEAR 9 - REASONING WITH NUMBER...

@whisto_maths

Using Percentages

What do I need to be able to do?

By the end of this unit you should be able to:

- Use FDP equivalence
- Calculate percentage increase and decrease
- Express percentage change
- Solve reverse percentage problems
- Solve percentage problems (calculator and non calculator problems)

Keywords

Percent: parts per 100 — written using the / symbol

Decimal: a number in our base 10 number system. Numbers to the right of the decimal place are called decimals. **Fraction:** a fraction represents how many parts of a whole value you have.

ı **1 Equivalent**: of equal value.

Reduce: to make smaller in value.

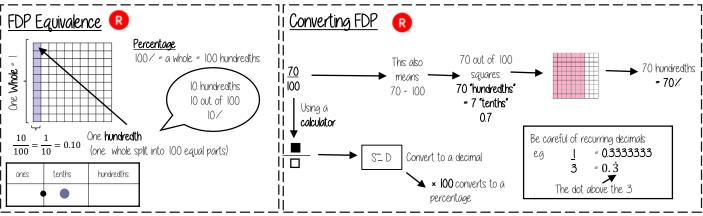
Growth: to increase / to grow.

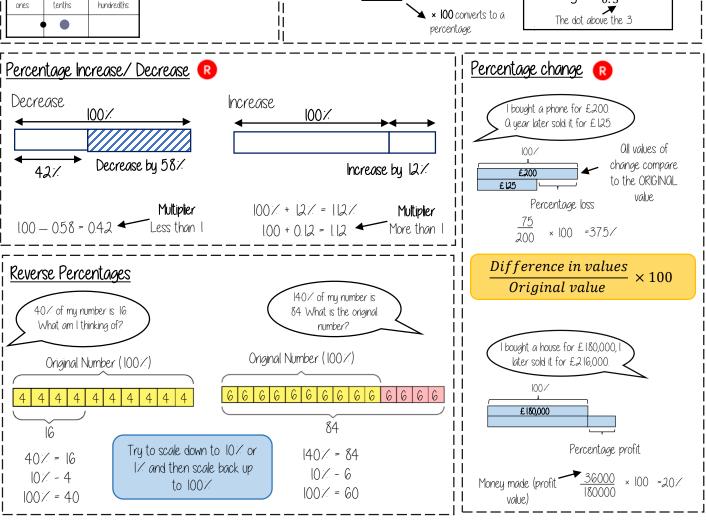
Integer: whole number, can be positive, negative or zero.

Invest: use money with the goal of it increasing in value over time (usually in a bank).

Multiplier: the number you are multiplying by.

| **Profit**: the income take away any expenses/costs.





YEAR 9 - REASONING WITH NUMBER.

@whisto_maths

Maths & Money

What do I need to be able to do?

By the end of this unit you should be able to:

- Solve problems with bills and bank statements
- Calculate simple interest
- Calculate compound interest
- Calculate wages and taxes
- Solve problems with exchange rates
- Solve unit pricing problems

<u>Keywords</u>

Credit: money being placed into a bank account

Debit: money that leaves a bank account **Balance**: the amount of money in a bank account

Expense: a cost/outgoing.

Deposit: an initial payment (often a way of securing an item you will later pay for)

Multiplier: a number you are multiplying by (Multiplier more than I = increasing, less than I = decreasing)

Per Onnum: each year

Currency: the type of money a country uses.

Unitary: one — the cost of one.

Bills and Bank Statements

Bills — tell you the amount items cost and can show how

much money you need to pay.

Some can include a total

Some can include a total
Look for different units
(Is it in pence or pounds)

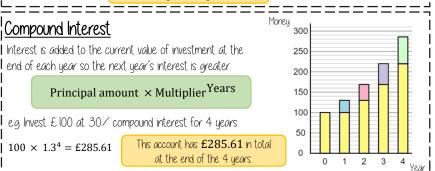
Menu	Price
Milk	89p
Tea	£1.50

Bank Statements

Bank statement can have negative balances if the money spent is higher than the money coming into the account

Date	Description	Credit	Debit	Balance
19th Sept	Salary	£1500		£1500
l9th Sept	Mortgage		£600	£900
25 th Setp	Bday Money	£15		£915

Simple Interest For each year of investment the interest remains the same Principal amount ×Interest Rate × Years 100 Principal amount is the amount invested in the account. I e.g. Invest £ 100 at 30 / simple interest for 4 years This account earned £120 interest Ot the end of year 4 they have £220 On 1 2 3 4 Year



Value Odded Tax (VOT)

VOT is payable to the government by a business. In the UK VOT is 20% and added to items that are bought.

Essential items such as food do not include VOT.

Wages and Taxes

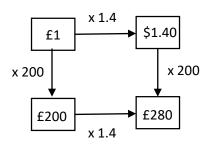
Salaries fall into tax brackets — which means they pay this much each month from their salary.

Taxable Income	Tax Rate
£12 501 to £50 000	20%
£50 001 to £150 000	40%
over £150 000	45%

Over time:

Time and a half — means 1.5 times their hourly rate





When making estimates it is also useful to use <u>estimates</u> to check if our solution is reasonable.

Use inverse operations to reverse the exchange process

Common Currencies		
United Kingdom	£	Pounds
United States of America	\$	Dollars
Europe	€	Euros

Unit Pricing

4 Oranges £1 5 cupcakes £1.20

4 = £1.00 $\div 2$ 5 = £1.20 $\div 5$ 1 = £0.25 $\div 2$ 1 = £0.20

 $\cancel{\cancel{\hspace{1cm}}}$ $\cancel{\cancel{\hspace{1cm}}}$ $\cancel{\hspace{1cm}}$ $\cancel{\hspace{1cm}}$

To calculate unit per cost you divide by the cost.

Cupcakes are the best value as one item has the cheapest value

There is a directly proportional relationship between the cost and number of units

YEAR 9 - REASONING WITH GEOMETRY

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Deduction

What do I need to be able to do?

By the end of this unit you should be able to:

- Identify angles in parallel lines
- Solve anale problems
- Make conjectures with angles
- Make conjectures with shapes

Keywords

Parallel: two straight lines that never meet with the same gradient.

Perpendicular: two straight lines that meet at 90°

Transversal: a line that crosses at least two other lines.

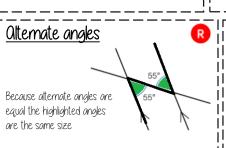
Sum: the result of adding two or more numbers.

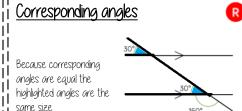
Conjecture: a statement that might be true but is not proven.

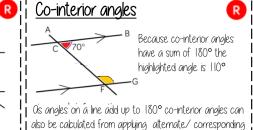
Equation: a statement that says two things are equal

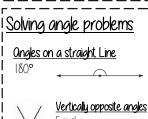
Polygon: a 2D shape made from straight edges.

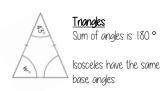
Counterexample: an example that disproves a statement











Link angle facts to algebra

 $2x + 4x = 180^{\circ}$

Form an equation State the reason

The sum of anales on a straight line is 180°

 $2x + 4x = 180^{\circ}$ $6x = 180^{\circ}$

 $x = 30^{\circ}$

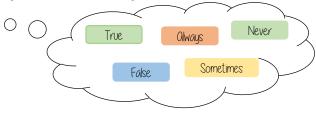
Interior Ongles

The angles enclosed by the polygon

(number of sides -2) x 180

Making conjectures with angles

Ongles around a point



Proving a conjecture

a pattern is noticed for many cases

disprove a conjecture

Apply the angle rules

The sum of angles in a triangle is 180°

Test the theory

180 - 70 - 20 = 90180 - 85 - 5 = 90

180 - 45 - 45 = 90

Make conjecture

Disproving a conjecture

Only one counterexample is needed to

The anale that meets the circumference in a semi circle is 90

Making conjectures with shapes

Keywords and facts to recall with shape

Orea: the amount of space inside a shape Perimeter: the length around a shape Regular Polygons: All sides and angles are equal

Quadrilateral Facts





<u>Parallelogram</u>

Opposite sides are parallel Opposite angles are equal Co-interior angles



Oll angles 90° Opposite sides are parallel



Oll sides equal size Opposite angles are equal



Kite

No parallel lines Equal lengths on top sides Equal lengths on bottom One pair of equal angles

YEAR 9 — REASONING WITH GEOMETRY... Rotation & Translation

@whisto maths

What do I need to be able to do?

By the end of this unit you should be able to:

- Identify the order of rotational symmetry
- Rotate a shape about a point on the
- Rotate a shape about a point not on a
- Translate by a given vector
- Compare rotations and reflections

Keywords

Rotate: a rotation is a circular movement

Symmetry: when two or more parts are identical after a transformation.

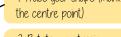
Reaular: a regular shape has angles and sides of equal lengths. **Invariant**: a point that does not move after a transformation.

Vertex: a point two edges meet. Horizontal: from side to side

Vertical: from up to down

Rotational Symmetry



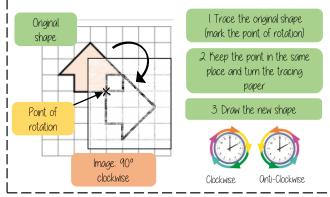




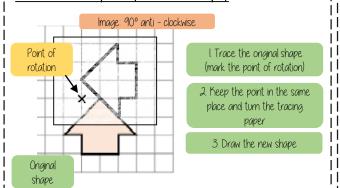
3. Count the times it fits back into itself

O regular pentagon has rotational symmetry of order 5

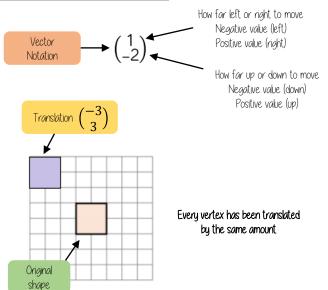
Rotate from a point (in a shape)



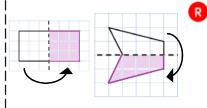
Rotate from a point (outside a shape)



Translation and vector notation



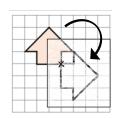
Compare rotations and reflections



Reflections are a mirror image of the original shape.

Information needed to perform a reflection

- Line of reflection (Mirror line)



Rotations are the movement of a shape in a circular motion

Information needed to perform a rotation:

- Point of rotation
- Direction of rotation
- Degrees of rotation

YEAR 9 — REASONING WITH GEOMETRY... Pythagoras' theorem

What do I need to be able to do?

By the end of this unit you should be able to:

- Use square and cube roots
- Identify the hypotenuse
- Calculate the hupotenuse
- Find a missing side in a Right angled
- Use Pythagoras' theorem on axes
- Explore proofs of Pythagoras' theorem.

Keywords

Square number: the output of a number multiplied by itself

Square root: a value that can be multiplied by itself to give a square number

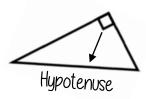
Hupotenuse: the largest side on a right angled triangle. Olways opposite the right angle.

Opposite: the side opposite the anale of interest

Odjacent: the side next to the angle of interest

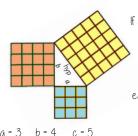
Squares and square roots is the square root symbol This can also be written as 6^2 eg $\sqrt{64} = 8$ Because 8 × 8 = 64 5 × 5 10 × 10 4 16 25 36 49 64 81 100 Square numbers

Identify the hypotenuse



The hypotenuse is always the longest side on a triangle because it is opposite the biggest angle.





If a triangle is right-angled, the sum of the squares of the shorter sides will equal the square of the hypotenuse.

$$a^2 + b^2 = \text{hypotenuse}^2$$

$$eg \ a^2 + b^2 = hypotenuse^2$$

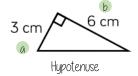
$$3^{2} + 4^{2} = 5^{2}$$

$$9 + 16 = 25$$

Substituting the numbers into the theorem shows that this is a right-angled triangle

Polygons can still have a hypotenuse if it is split up into 1 triangles and opposite a right

Calculate the hypotenuse



Either of the short sides can be labelled a or b

 $a^2 + b^2 = \text{hypotenuse}^2$

I Substitute in the values for a and b

 3^2+6^2 = hypotenuse²

 $9 + 36 = \text{hypotenuse}^2$

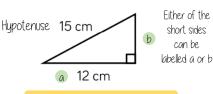
 $45 = hypotenuse^2$

2. To find the hypotenuse square root the sum of the squares of the shorter sides.

 $\sqrt{45}$ = hypotenuse

6.71cm = hypotenuse

Calculate missing sides



 $a^2 + b^2 = \text{hypotenuse}^2$

$$12^2+b^2=15^2$$

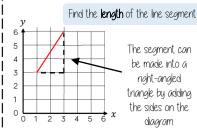
I Substitute in the values you are given

 $144 + b^2 = 225$

Rearrange the equation by subtracting the shorter square from the hypotenuse squared

 $b^2 = 111$ Square root to find the length $b = \sqrt{111} = 10.54 \ cm$ of the side

Pythagoras' theorem on a coordinate axis



The line segment is the hypotenuse

$$a^2 + b^2 = \text{hypotenuse}^2$$

The lengths of a and b are the sides of the triangle.

Be careful to check the scale on the axes

YEAR 9 - REASONING WITH GEOMETRY ...

@whisto_maths

Enlargement & Similarity

What do I need to be able to do?

By the end of this unit you should be able to:

- Recognise enlargement and similarity
- Enlarge a shape by a positive SF
- Enlarge a shape from a pointEnlarge a shape by a fractional SF
- Work out missing sides and angles in a pair of similar shapes.

<u>Keywords</u>

Similar Shapes: shapes of different sizes that have corresponding sides in equal proportion and identical corresponding angles.

Scale Factor: the multiple describing how much a shape has been enlarged

Enlarge: to change the size of a shape (enlargement is not always making a shape bigger)

Enlarge a shape from a point

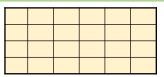
Scaled distances method

Corresponding: objects (or sides) that appear in the same place in two similar situations. **Image:** the picture or visual representation of the shape

Recognise enlargement & similarity

Shapes are similar if all pairs of corresponding sides are in the same ratio

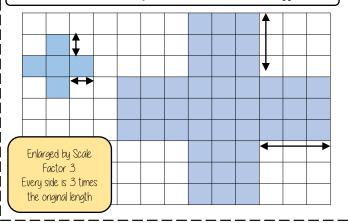
These shapes are similar because all sides are increased by the same ratio



Enlargements are similar shapes with a ratio other than I

Enlarge by a positive scale factor

With a scale factor larger than 1 it makes the shape **bigger**

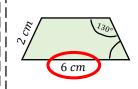


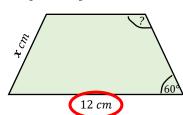
Scale the distance between the point of

enlargement and each corresponding

Don't forget that properties of shapes don't change with enlargements or in

The two trapezium are similar find the missing side and angle





Raus method

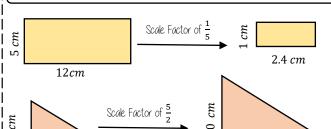
Multiply the distance from the centre of

corresponding vertices by the scale factor along the ray

Positive fractional scale factor

10 cm

With a scale factor between 0 and 1 it makes the shape **smaller**



25 cm

the scale factor

Corresponding sides identify

$$\frac{12}{6} = 2$$

Scale Factor = 2

Calculate the missing side

Length (corresponding side) x scale factor

 $2cm \times 2$

x = 4cm

Enlargement does not change angle size

Calculate the missing angle Corresponding angles remain the same 130°

YEAR 9 - REASONING WITH GEOMETRY

@whisto maths

Solving ratio & proportion problems

What do I need to be able to do?

By the end of this unit you should be able to:

- Solve problems with direct proportion
- Use conversion graphs
- Solve problems with inverse proportion
- Solve ratio problems
- Solve 'best buy' problems

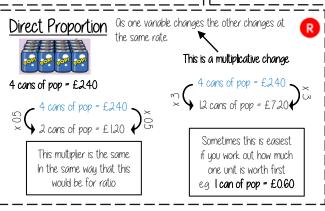
!! <u>Keywords</u>

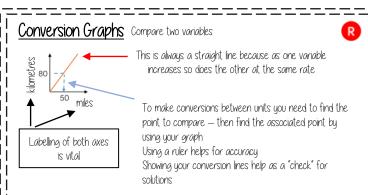
Proportion: a comparison between two numbers

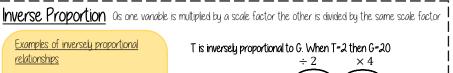
Ratio: a ratio shows the relative size of two variables

Direct proportion: as one variable is multiplied by a scale factor the other variable is multiplied by the same scale factor.

Inverse proportion:: as one variable is multiplied by a scale factor the other is divided by the same scale factor.



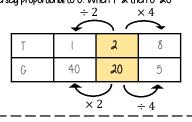




Sharing a whole into a given ratio 🕟 🛛 Finding a value given In (or n. 1)

Time taken to fill a pool and the number of taps running.

Time taken to paint a room and the number of workers



Inside a box are blue and red pens in the ratio 5:1

If there are 10 red pens how many blue pens are there?

Blue pens

One unit

Model the Question

Blue: Red



To calculate best buys you need to be able to

compare the cost of one unit or units of

equal amounts

Cost per item

Best Buys

I can is £0.30 I can is £0.31 Or 30p Or 3 lp

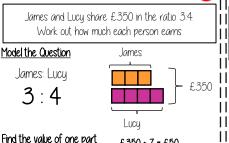
Have a directly proportional relationship

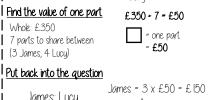
Shop Ais the best value as it is lp cheaper per can of pop

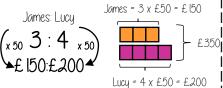


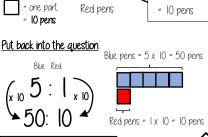
Shop ${\sf A}$ is still shown as being the best value but pay attention to the unit you are calculating, per item or per pound.

Best value is the most product for the lowest price per unit









There are 50 Blue Pens

YEAR 9 - REASONING WITH GEOMETRY.

@whisto_maths

Rates

÷ 60

hours

minutes

What do I need to be able to do?

By the end of this unit you should be able to:

- Solve speed, distance, time questions
- Use distance time graphs
- Solve density, mass, volume problems
- Solve flow problems
- Use flow graphs
- Interpret rates of change and their units

<u>Keywords</u>

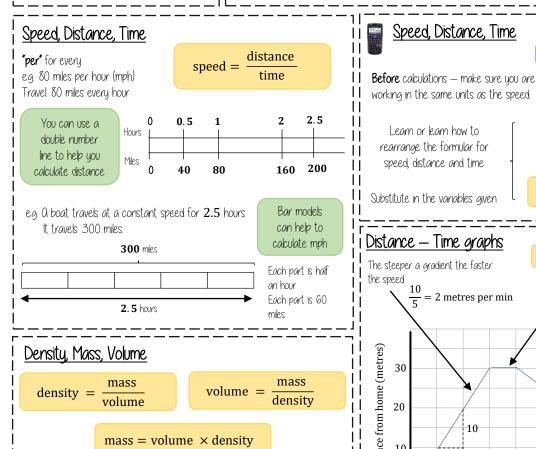
Convert: change

Mass: a measure of how much matter is in an object. Commonly measured by weight.

Origin: the coordinate (0, 0)

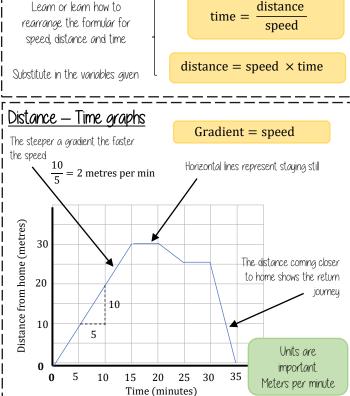
Volume: the amount of 3D space a shape takes up

Substitute: putting numbers where letters are — replacing numbers into a formula



Orea of cross

section



Flow problems & graphs

speed up and the neck of the bottle fill at a faster constant speed

The culinder will fill at a constant speed

Units are im

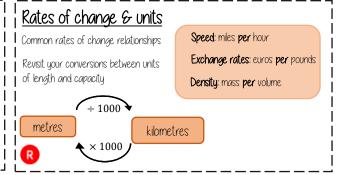
This will fill at a constant rate, then as the space decreases it will

ymaer will till at a corista

volume of prism

Units are important Ensure any volume calculations are the same unit as the rate of flow

× Depth



YEAR 9 - REPRESENTATIONS.

@whisto maths

Probability

What do I need to be able to do?

By the end of this unit you should be able to:

- Find single event probability
- Find relative frequency
- Find expected outcomes
- Find independent events
- Use diagrams to work out probabilities

Keywords

Probability: the chance that something will happen

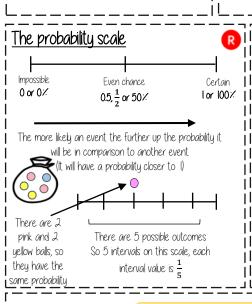
Relative Frequency: how often something happens divided by the outcomes

Independent: an event that is not effected by any other events.

Chance: the likelihood of a particular outcome.

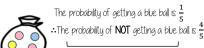
Event: the outcome of a probability — a set of possible outcomes.

Biased: a built in error that makes all values wrong by a certain amount.



🔃 I Single event probabilitu

Probability is always a value between 0 and 1



The sum of the probabilities is 1

The table shows the probability of selecting a type of chocolate

Dark	Milk	White
0.15	0.35	

P(white chocolate) = 1 - 0.15 - 0.35



Relative Frequency

Frequency of event Total number of outcomes

Remember to calculate or identify the overall number of outcomes!

Colour	Frequency	Relative Frequency
Green	6	0.3
Yellow	12	0.6
Blue	2	0.1
	20	

Relative frequency can be used to find expected

e.g. Use the relative probability to find the expected outcome for green if there are 100 selections.

Relative frequency x Number of times $0.3 \times 100 = 30$

Expected outcomes

Expected outcomes are estimations. It is a long term average rather than a prediction.

Dark	Milk	White	
0.15	0.35	0.5	

The sum of the probabilities is 1

On experiment is carried out 400

Show that dark chocolate is expected to be selected 60 times

 $0.15 \times 400 = 60$

Independent events



The rolling of one dice has no impact on the rolling of the other. The individual probabilities should be calculated separately.

Probability of event 1 × Probability of event 2



$$P(5) = \frac{1}{6}$$

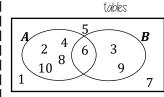
$$P(5) = \frac{1}{6}$$
 $P(R) = \frac{1}{4}$

Find the probability of getting a 5 and

$$P(5 \text{ and } R) = \frac{1}{6} \times \frac{1}{4} = \frac{1}{24}$$

Using diagrams Recap Venn diagrams, Sample space diagrams and Two-way

Ш



Car		Bus	Walk	Total	
Boys 15		24	14	53	
Girls 6		20	21	47	
Total	21	44	35	100	

The possible outcomes from rolling a dice

\equiv	Ş					1		
. OUTCOM	tossing a coir		1	2	3	4	5	6
he possible from tossir	Н	ľΉ	2,H	3,H	4,H	5,H	6,H	
	from	Τ	ļΤ	2,T	3,T	4,T	5,T	6,T

YFAR 9 - REPRESENTATIONS

@whisto maths

Algebraic Representation

What do I need to be able to do?

By the end of this unit you should be able to:

- Draw quadratic graphs
- Interpret quadratic graphs
- Interpret other graphs including reciprocals
- Represent inequalities

Keywords

Quadratic: a curved graph with the highest power being 2. Square power.

Inequality: makes a non equal comparison between two numbers

Reciprocal: a reciprocal is 1 divided by the number

Cubic: a curved graph with the highest power being 3. Cubic power.

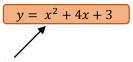
Origin: the coordinate (0, 0)

Parabola: a 'u' shaped curve that has mirror symmetry

Intersection with

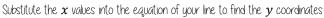
the γ axis

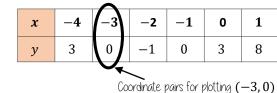
Quadratic Graphs



If x^2 is the highest power in your equation then you have a quadratic graph.

It will have a parabola shape





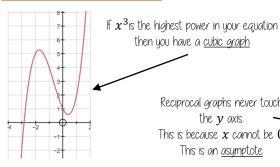
Plot all of the coordinate pairs and join the points with a curve (freehand)

Quadratic graphs are always symmetrical with the turning point in the middle

Interpret other graphs

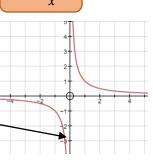
Cubic Graphs

$$y = x^3 + 2x^2 - 2x + 1$$

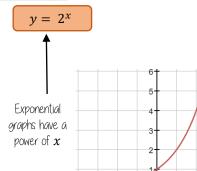




Reciprocal Graphs



Exponential Graphs



Reciprocal graphs never touch the ν axis.

then you have a <u>cubic graph</u>

This is because x cannot be 0

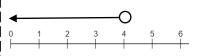
This is an asymptote

Represent Inequalities

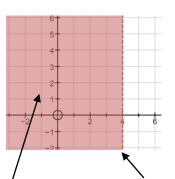
Multiple methods of representing inequalities



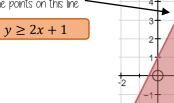
Oll values are less than 4



The shaded area indicates all possible values of x



The solid line shows that the inequality includes all the points on this line



The shaded area indicates all possible solutions to this inequality

The dotted line shows that the inequality does not include these points